

Example:

Rolling a die is an experiment.

The different faces on the die are its outcomes. Sample space =  $\{ 1, 2, ..., 6 \}$ 

An event, for example, could be rolling an odd number.  $E = \{ 1, 3, 5 \}$ 

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The probability of an <u>event</u> occurring in an <u>experiment</u> is also a number between (and possibly equal to) 0 and 1.

It is written P(E).

**EMPIRICAL ASSIGNMENT OF PROBABILITIES** If *E* is an event and we perform an experiment several times, then we estimate the probability of *E* as follows:  $P(E) = \frac{\text{the number of times } E \text{ occurs}}{\text{the number of times the experiment is performed}}.$ This ratio is sometimes called the *relative frequency* of *E*.

Example: Experiment is roll a die.

Sample space: { 1, 2, 3, 4, 5, 6 }

What is the probability of rolling an odd number?

Example: Experiment is roll a die.

Sample space: { 1, 2, 3, 4, 5, 6 }

What is the probability of rolling an odd number?

Event E = { 1, 3, 5 }

P(E) = 3/6 = 1/2

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A drug was given with the following A drug was given with the following results: results: Number of Number of **Side Effects** Side Effects Times Times None None 72 72 Mild 25 Mild 25 Severe 3 Severe 3 What is the probability of severe side What is the probability of severe side effects? effects? the number of times severe side effects occurred P(severe side effects) =the number of times the experiment was performed  $=\frac{3}{100}=0.03$ 11

experiments. These are called <b>empirical</b> <b>probabilities</b> . Example: Everyone in the class flip a coin. Enter 1 for Heads, 2 for Tails.	combinatorial formulas. These are called <b>theoretic probabilities</b> . Example: An experiment involves flipping a coin. The event E = {Heads} Find P(E).
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Example:	Example:
Flip 3 fair coins. What is the probability of getting exactly two heads?	Flip 3 fair coins. What is the probability of getting exactly two heads?
	Sample space = {HHH,HHT,HTH,HTT,THH,THT,TTH,TTT} Event E = {HHT, HTH, THH}
	P(E) = 3/8
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Example:	We can use counting methods to
Flip 3 fair coins. What is the probability of getting exactly two heads?	determine both the size of the sample space, and the size of the event space to compute P(E).
Let's do this empirically – as in do this experiment ourselves.	
Click in the number of heads you get when flipping a coin 3 times.	<b>CALCULATING PROBABILITY WHEN OUTCOMES ARE EQUALLY</b> <b>LIKELY</b> If <i>E</i> is an event in a sample space <i>S</i> with all <i>equally likely outcomes</i> , then the probability of <i>E</i> is given by the formula: $P(E) = \frac{n(E)}{n(S)}.$
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2 roomates are selected from 2 male and 3 female applicants. If chosen at random, what is the probability that both are female? 2 roomates are selected from 2 male and 3 female applicants. If chosen at random, what is the probability that both are female?

Sample space = 2 chosen from 5 people

Event = 2 of the 3 females chosen

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2 roomates are selected from 2 male and 3 female applicants. If chosen at random, what is the probability that both are female?

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Sample space = 2 chosen from 5 people

Size = 
$$C(5,2) = 10$$

Event = 2 of the 3 females chosen

Size = C(3,2) = 3

P(E) = 3/10

Roll a die 2 times. What is the probability that the sum is 4?



Sample space = roll a die twice

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Event E = \{ (1,3), (2,2), (3,1) \}
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## **Probability and Genetics**

Between 1856 and 1863, Gregor Mendel cultivated some 29,000 pea plants.

He discovered characteristics (that we now call genes) passed from parent to offspring.



One focus was on color. One gene, yellow seemed to be *dominant*. The other, green, seemed to be *recessive*.

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If one parent has genes AB, and another has genes MN then the offspring would have one of:

AM BM AN BN

We will use uppercase for dominant genes and lowercase for recessive genes.

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If both parents have Yg genes, what is the probability that the child of yellow pea plants is green?

If both parents have Yg genes, what is the probability that the child of yellow pea plants is green?

P(E) = 1/4



If a family has three children, what are the odds **for** all three children being the same gender?

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E = same gender
= { bbb, ggg }
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E' = complement = not all the same = { bbg, bgb, bgg, gbb, gbg, ggb }

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1:3 for

## Odds

• Example: A roulette wheel has 38 equal-size compartments. Thirty-six of the compartments are numbered 1 to 36 with half of them colored red and the other half black. The remaining 2 compartments are green and numbered 0 and 00. A small ball is placed on the spinning wheel and when the wheel stops, the ball rests in one of the compartments. What are the odds against the ball landing on red?

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Odds	Odds
Solution:	Solution:
There are 38 equally likely outcomes.	There are 38 equally likely outcomes. 18 are in favor of the event "the ball lands on red" and 20
Event E = "the ball lands on red"	are against the event.
Event E' = the opposite	The odds against red are 20 to 18 or 20:18, which we reduce to 10:9.
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